



# COMPUTER GRAPHICS

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# Course overview

- Introduction to Computer Graphics
- Video Display Device
- Random Scan & Raster Scan
- Color CRT Monitors
- Line drawing Algorithms
- Circle Drawing Algorithm
- Polygon Filling Algorithms
- 2D Transformations
- Homogenous Coordinates
- Composite Transformations
- Window to View Port Transformations
- Clipping
- 3D Transformations
- Projections
- Hidden Surface Removal Methods
- Color Spaces & Illumination Models
- Polygon Rendering Methods
- Animation Sequences

# What is Computer Graphics?



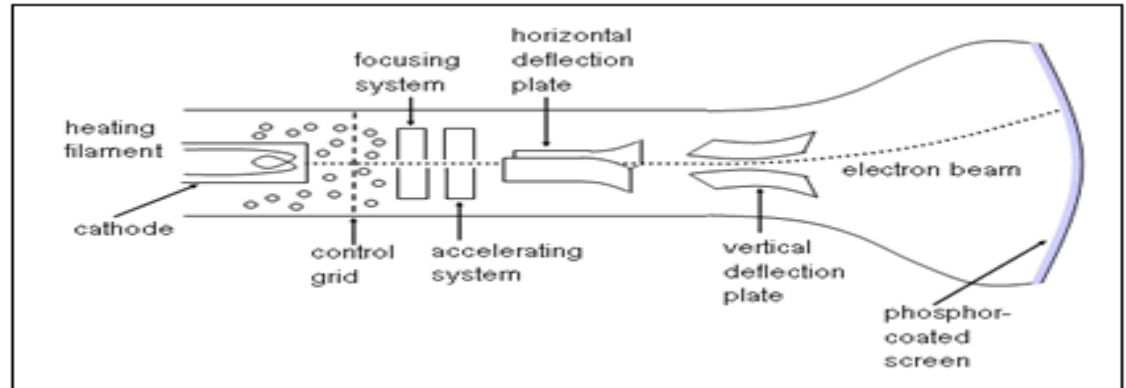
Computer graphics is a field of computer science, which deals with creation, representation and management of images on the computer screen.

## **Applications**

- ✓ graphical user interface
- ✓ Computer-Aided Design
- ✓ Image Processing
- ✓ Entertainment
- ✓ Computer Art and commerce
- ✓ Simulation and modeling
- ✓ Cartography
- ✓ Scientific and business Visualization

# Video Display Devices

Primary output device in a graphics system is a video monitor. The operation of most video monitors is based on the standard Cathode Ray Tube (CRT).



## Working Principle

- A beam of electrons (cathode rays), emitted by an electron gun, passes through focusing and deflection system that direct the beam toward specified positions on the phosphor-coated screen. The phosphor then emits a small spot of light at each position contacted by the electron beam.
- This type of display is called Refresh CRT.

# Measurement of Performance



## **Persistence**

Persistence is defined as the time it takes the emitted light from the screen to decay one-tenth of its original intensity.

## **pixel**

A pixel is a smallest addressable screen element. On the monitor of a computer, a pixel is usually a square. Every pixel has a color and all the pixel together forms the picture.

## **Resolution**

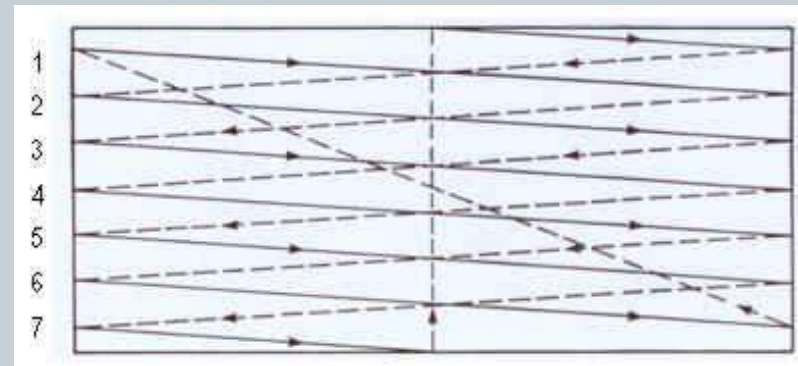
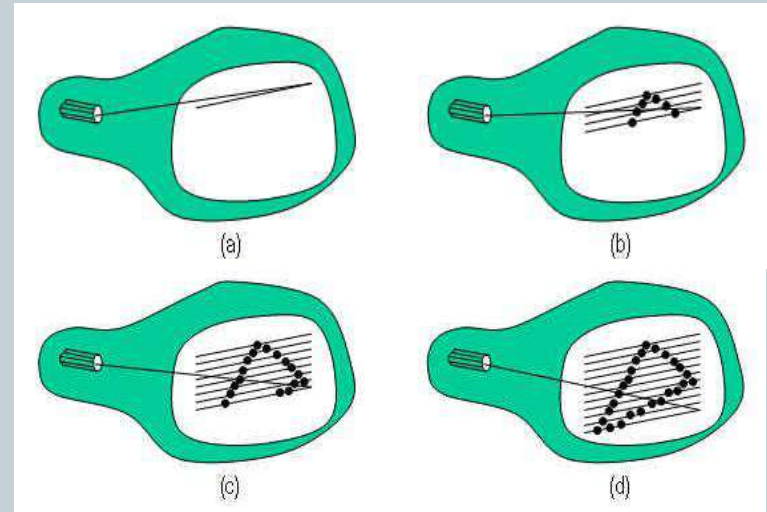
Resolution refers to the sharpness and clarity of an image. Resolution indicates the maximum number of points that can be displayed without overlap on a CRT.

## **Aspect Ratio**

Aspect ratio of an image or a screen is a proportional relationship between its width and height. Or This number gives the ratio of horizontal points to vertical points of an image or screen.

# Raster Scan Displays.

- In this electron beam is swept across the screen one row at a time from top to bottom.
- As beams moves across each row, the beam intensity is turned on and off to create a pattern of illuminated spots.
- Picture definition is stored in a memory area called the **frame buffer**.
- It well suited for the realistic display of scenes.
- The return of beams to the left of the screen, after refreshing each scan line, is called the **horizontal retrace** .
- At the end of each frame, the electron beam returns the top left corner of the screen to begin the next frame is called vertical retrace.

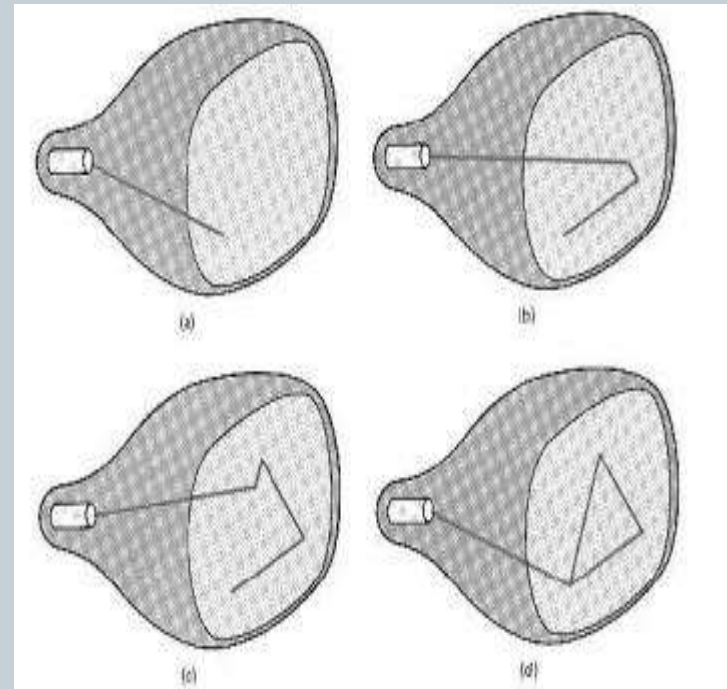




# Random Scan Display

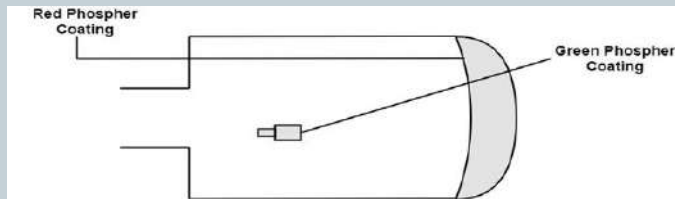


- Here electron beam is directed to only those parts of the screen where a picture is to be drawn.
- The picture definition is stored as a set of line-drawing commands in a refresh display file or a refresh buffer .
- Higher resolution than raster systems and can produce smooth line drawings.
- Also called **vector displays** or **stroke writing displays**.



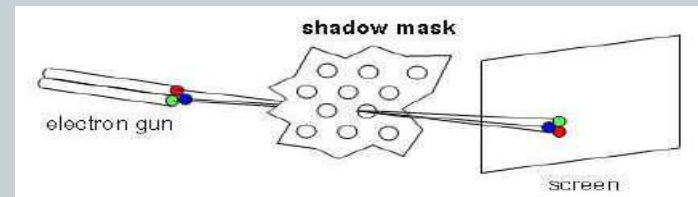
# Color CRT Monitors

## Beam Penetration Method



- Random scan monitors use the beam penetration method for displaying color picture.
- Inside of CRT screen is coated two layers of phosphor namely red and green.
- It can produce maximum of 4 colors.
- Less Expensive
- Quality of picture is not much as good as another method.

## Shadow Mask Method



- Raster scan systems use shadow mask methods to produce a much more range of colors.
- In this, CRT has three phosphor color dots, one emits a red, second emits green and third emits a blue light.
- produce realistic images using millions of colors and shadows scenes.
- Expensive
- Poor Resolution



# Digital Differential Analyzer (DDA) Algorithm



- DDA is a scan conversion line algorithm.
- Given Starting and ending coordinates of a line  $(X_0, Y_0)$  and  $(X_n, Y_n)$ .
- This algorithm attempt to generate points between starting and ending coordinates.

## Steps

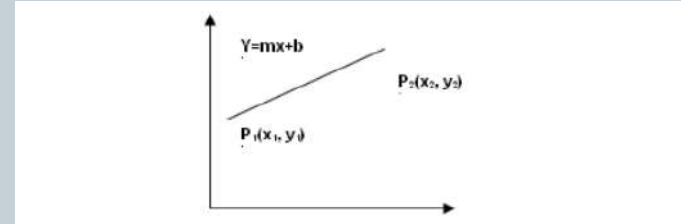
1. Calculate  $D_x, D_y$  and  $M$  from the given input.

$$D_x = X_n - X_0, \quad D_y = Y_n - Y_0, \quad M = D_y / D_x$$

2. If  $(\text{absolute}(D_x) > \text{absolute}(D_y))$  then

$$\text{steps} = \text{absolute}(D_x);$$

Else  $\text{steps} = \text{absolute}(D_y);$



3. If current point is  $(X_k, Y_k)$  then next point is  $(X_{k+1}, Y_{k+1})$ .

There are three cases.

- ✓ Case 1: If  $M < 1$ , then  $X_{k+1} = \text{roundoff}(1 + X_k)$   
 $Y_{k+1} = \text{roundoff}(M + Y_k)$ .
- ✓ Case 2: If  $M > 1$ , then  $X_{k+1} = \text{roundoff}(1/M + X_k)$   
 $Y_{k+1} = \text{round off}(1 + Y_k)$ .
- ✓ Case 3: If  $M = 1$ , then,  $X_{k+1} = \text{roundoff}(1 + X_k)$   
 $Y_{k+1} = \text{round off}(1 + Y_k)$ .
- Repeating the above step until the end points is reached

# Bresenham's Line Algorithm

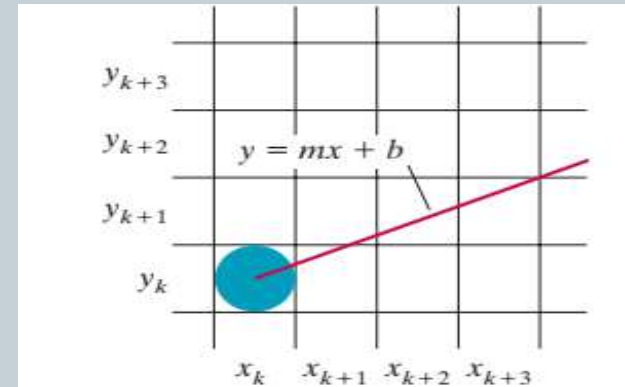
This algorithm is very efficient since it scan convert lines using only incremental integer calculations, so can be adapted to display circles and other curves.

- Input the two line end points and store the left end points in  $(X_0, Y_0)$ .
- Set the color for frame buffer position  $(X_0, Y_0)$  that is plot the first point.
- Calculate the constants  $D_x, D_y$ , and starting value for Decision parameter  $P_0 = 2D_y - D_x$ .
- At each  $X_k$  along the line starting at  $k= 0$  Perform the following task,

If  $P_k < 0$ , the next point to plot is  $(X_k + 1, Y_k)$  and  $P_{k+1} = P_k + 2D_y$ .

Otherwise next point to plot is  $(X_k + 1, Y_k + 1)$   
 $P_{k+1} = P_k + 2D_y - 2D_x$ .

- Perform the above step until the end point is reached or  $D_x - 1$  times.



## Advantages

- It is easy to implement and fast.
- It uses fixed points only and more accurate than DDA algorithm.

## Disadvantages

- The resulted line is not smooth.
- This algorithm is for basic line drawing and cannot handle diminishing jaggies.

# Midpoint Circle Algorithm

- The midpoint circle algorithm is an incremental algorithm for drawing circles.
- Here we use eight-way symmetry .
- So only calculate the points for the top right eighth of a circle, and then use symmetry to get the rest of the points.
- The equation of circle centered at origin and radius  $r$  is given by
- $$f_{\text{circle}}(x,y) = x^2 + y^2 - r^2$$

## Procedure

Step 1: Input radius  $r$ , and circle center  $(x_c, y_c)$  then set coordinates for the first point on the circumference of a circle centered on the origin as,

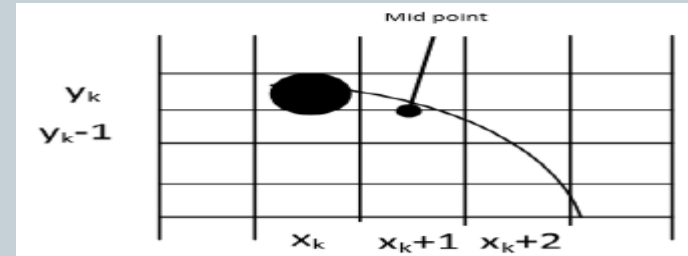
$$(x_0, y_0) = (0, r)$$

Step 2: Calculate initial value of decision parameter as

$$P_0 = 5/4 - r$$

Step 3: At each  $X_k$  along the line starting at  $k=0$  Perform the following task,

If  $P_k < 0$ , the next point to along the circle is  $(x_{k+1}, y_k)$  and  $P_{k+1} = P_k + 2x_{k+1} + 1$ .



Otherwise  $(x_k + 1, y_k - 1)$  and  $P_{k+1} = P_k + 2x_{k+1} + 1 - 2y_{k+1}$   
 where  $2x_{k+1} = 2x_k + 2$  and  $2y_{k+1} = 2y_k - 2$

Step 4: Determine symmetry points in other seven octants.

Step 5: Move each calculated pixel position  $(x, y)$  onto the next point along the circle is the circular path centered at  $(x_c, y_c)$  and plot the coordinate values.

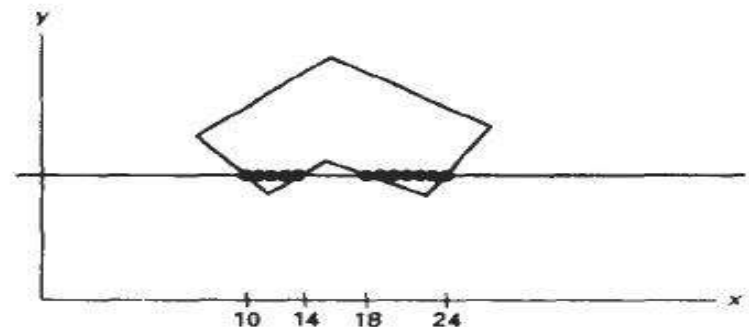
$$x = x + x_c, \quad y = y + y_c$$

Step 5: Repeat step 3 through 5 until  $x \geq y$ .

# Polygon Filling Algorithms



- A polygon can be represented as a group of connected edges, forming a closed figure.
- Polygon filling algorithms are used for coloring the area of the polygon.
- ✓ **In Scan-Line Polygon Fill Algorithm** For each scan line crossing a polygon, this algorithm locates the intersection points of the scan line with the polygon edges.
- ✓ These intersection points are then sorted from left to right, and the corresponding frame buffer positions between each intersection pair are set to the specified fill color.



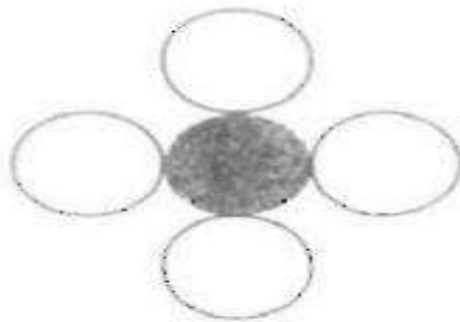
# Polygon Filling Algorithms



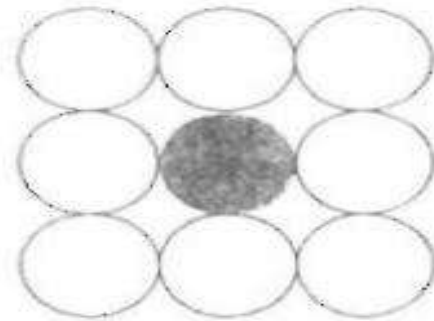
## Boundary Fill Algorithm

- The algorithms which are defining the boundary of the polygon are called boundary fill algorithm.
- In boundary filling method ,start from an interior point(seed) and paint interior outward towards the boundary.
- If the boundary is specified in a single color , the the fill algorithm proceeds outward pixel by pixel until the boundary color encountered.

4 Connected



8 Connected



# 2D Transformations

- Transformation is a process of modifying and repositioning the existing graphics.
- When a transformation takes place on a 2D plane, it is called 2D transformation.
- Basic Transformations are Translation, Rotation, Scaling.
- **Translation** is applied to an object by re-positioning it along a straight line path from one co-ordinate location to another.

## Translation

Here translate a two-dimensional point  $(x, y)$  by adding translation distances,  $t_x, t_y$  then getting a new position  $(x', y')$  as:

$$P = \begin{bmatrix} x \\ y \end{bmatrix} \quad P' = \begin{bmatrix} x' \\ y' \end{bmatrix} \quad T = \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

$$\therefore P' = P + T$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

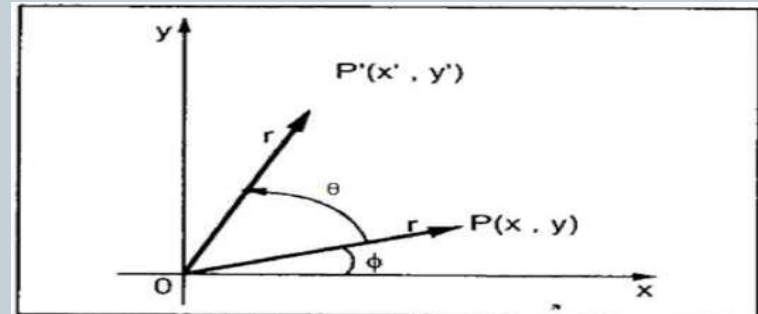


# 2D Transformations



## Rotation

- In rotation, we rotate the object at particular angle  $\theta$  (theta) from its origin along a circular path in XY plane. You will get a new point  $P'(X', Y')$ .



Using standard trigonometric,  $P(X, Y)$  can be represented as

$$x = r \cos \phi$$

$$y = r \sin \phi$$

$$x' = r \cos(\phi + \theta) = r \cos \phi \cos \theta - r \sin \phi \sin \theta$$

$$y' = r \sin(\phi + \theta) = r \cos \phi \sin \theta + r \sin \phi \cos \theta$$

Substituting value of  $x, y$  in  $x', y'$

$$\text{we get } x' = x \cos \theta - y \sin \theta$$

$$y' = x \sin \theta + y \cos \theta$$

Representing the above equation in matrix form,

$$[X' \ Y'] = [X \ Y] \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

OR

$$P' = P \cdot R, \text{ Where } R = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

# 2D Transformations



- A scaling transformation alters the size of the object.
- Scaling is carried out by multiplying the co-ordinate values  $(x, y)$  of each vertex by scaling factor  $s_x$  and  $s_y$  to produce transformed co-ordinates  $(x', y')$ .
- i.e.  $x' = x \cdot s_x$   
 $y' = y \cdot s_y$
- If both scaling factors have same value then the scaling is known as **uniform scaling**.
- Otherwise it is called differential Scaling.

## Scaling

- The matrix equation for scaling is:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix}$$

OR

$$P' = S \cdot P$$

# Homogenous Coordinates

- We can combine the multiplicative and translational terms for 2D geometric transformations into a single matrix representation by expanding 2x2 matrix to 3x3.

- In this way, we can represent the point by 3 numbers instead of 2 numbers, which is called Homogenous Coordinate system.

$$(x, y) \rightarrow (x_h, y_h, h)$$

- In this system, we can represent all the transformation equations in matrix multiplication.

## Translation

$$P' = T(t_x, t_y) \cdot P$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

## Rotation

$$P' = R(\theta) \cdot P$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

## Scaling

$$P' = S(S_x, S_y) \cdot P$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

# Composite Transformations

- It is sequence of geometric transformations.

Example :Animation

- **Translations**

If two successive translation vectors  $(t_{x1}, t_{y1})$  and  $(t_{x2}, t_{y2})$  are applied to a coordinate position  $P$ , the final transformed location  $P'$  is calculated as

$$P' = T(t_{x2}, t_{y2}) \cdot \{T(t_{x1}, t_{y1}) \cdot P\}$$

$$P' = \{T(t_{x2}, t_{y2}) \cdot T(t_{x1}, t_{y1}) \cdot P\}$$

$$\begin{bmatrix} 1 & 0 & t_{x2} \\ 0 & 1 & t_{y2} \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & t_{x1} \\ 0 & 1 & t_{y1} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_{x1} + t_{x2} \\ 0 & 1 & t_{y1} + t_{y2} \\ 0 & 0 & 1 \end{bmatrix}$$

$$T(t_{x2}, t_{y2}) \cdot T(t_{x1}, t_{y1}) =$$

$$T(t_{x1} + t_{x2}, t_{y1} + t_{y2})$$

which demonstrates that two successive translations are additive.

# Composite Transformations

## Rotation

- Two successive rotations applied to point  $\mathbf{p}$  produce the transformed position
$$\mathbf{P}' = \mathbf{R}(\theta_2) \cdot \{\mathbf{R}(\theta_1) \cdot \mathbf{P}\}$$
$$= \{\mathbf{R}(\theta_2) \cdot \mathbf{R}(\theta_1)\} \cdot \mathbf{P}$$
- By multiplying the two rotation matrices, we can verify that two successive rotations are additive:
$$\mathbf{R}(\theta_2) \cdot \mathbf{R}(\theta_1) = \mathbf{R}(\theta_1 + \theta_2)$$
- So that the final rotated coordinates can be calculated with the composite rotation matrix as
$$\mathbf{P}' = \mathbf{R}(\theta_1 + \theta_2) \cdot \mathbf{P}$$

## Scaling

- Concatenating transformation matrices for two successive scaling operations produces the following composite scaling matrix:

$$\begin{bmatrix} s_{x2} & 0 & 0 \\ 0 & s_{y2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} s_{x1} & 0 & 0 \\ 0 & s_{y1} & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} s_{x1} \cdot s_{x2} & 0 & 0 \\ 0 & s_{y1} \cdot s_{y2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$S(s_{x2}, s_{y2}) \cdot S(s_{x1}, s_{y1}) = S(s_{x1} \cdot s_{x2}, s_{y1} \cdot s_{y2})$$

- Indicates that successive scaling operations are multiplicative.

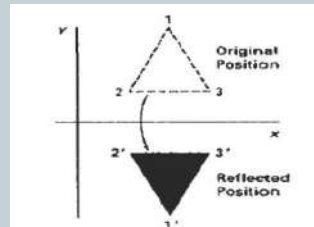
# Other Transformations

## Reflection

- Reflection is a transformation that produces a mirror image of an object.
- In 2D-transformation, reflection is generated relative to an axis of reflection.
- Relative axis of reflection, is same as 180° rotation about the reflection axis

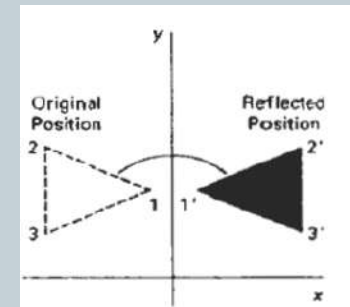
## Reflection about X-axis

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



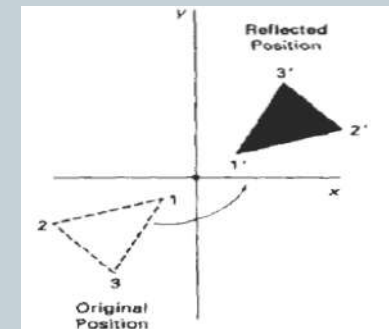
## Reflection about Y-axis

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



## Reflection about origin

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$





# Other Transformations

## Shearing

- A transformation that distorts the shape of an object is called shearing.

- **X-direction Shear** : shearing relative to x-axis is ,  
which transforms

$$x' = x + sh_x \text{ and } y' = y$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & s_{hx} & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- **Y-direction shear:**

Any-direction shear relative to y-axis which transforms

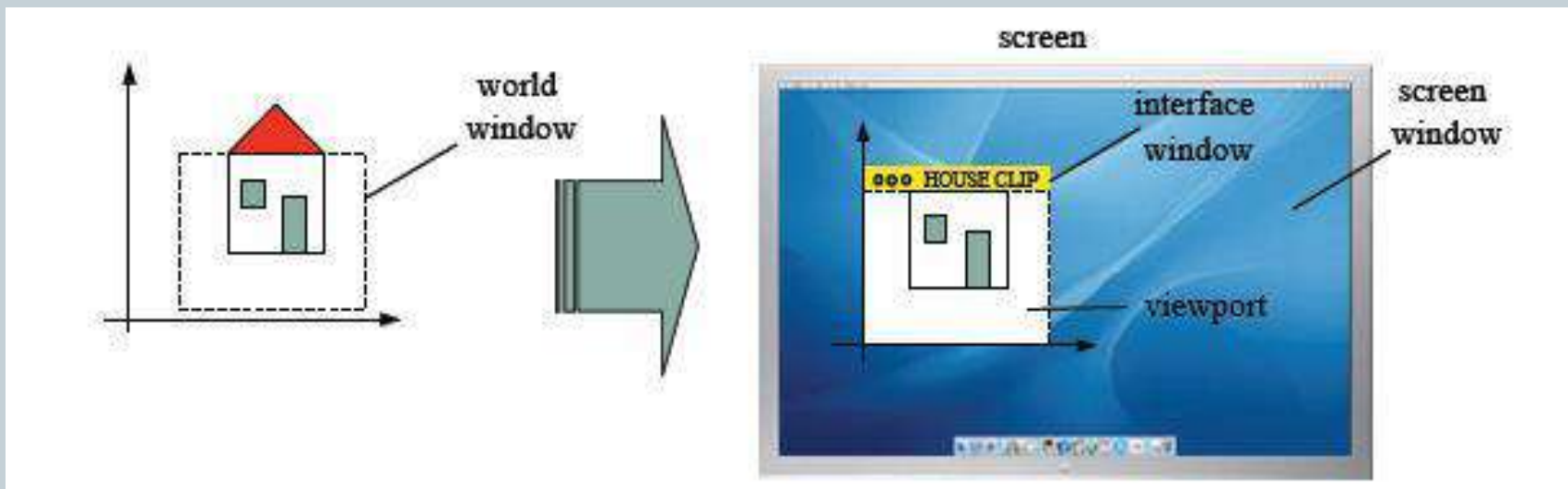
$$x' = x \text{ and } y' = x \cdot sh_y + y$$

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ s_{hy} & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

# Window to Viewport Transformation



- **Window:** A world-coordinate area selected for display.
- **Viewport:** An area on a display device to which a window is mapped.
- The window defines *what* is to be viewed
- the viewport defines *where* it is to be displayed



# Window to Viewport Transformation

- A point at position  $(x_w, y_w)$  in the window is mapped into position  $(x_v, y_v)$  in the associated viewport.

$$x_v = x_{v_{\min}} + (x_w - x_{w_{\min}})S_x$$

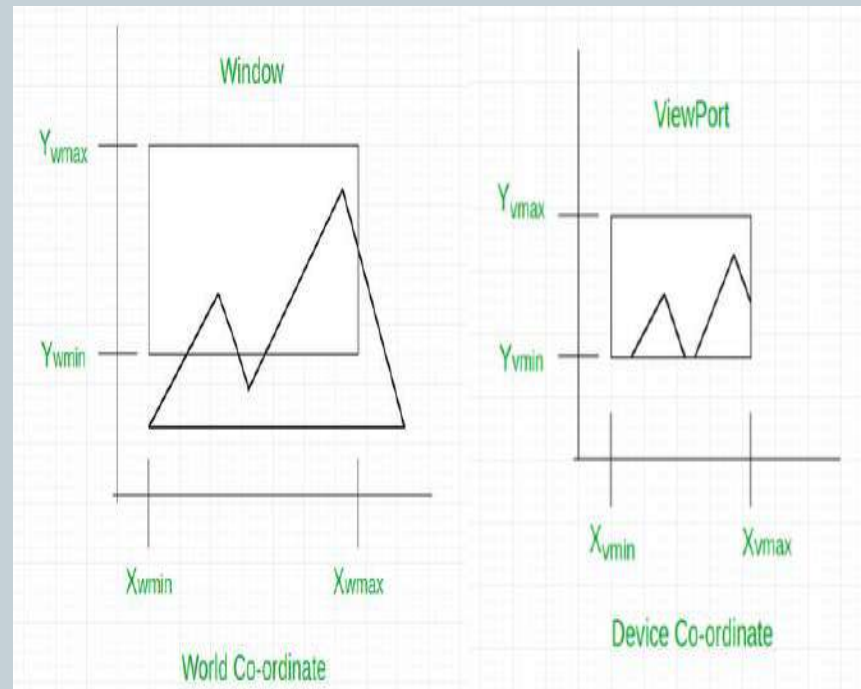
$$y_v = y_{v_{\min}} + (y_w - y_{w_{\min}})S_y$$

$$\frac{x_v - x_{v_{\min}}}{x_{v_{\max}} - x_{v_{\min}}} = \frac{x_w - x_{w_{\min}}}{x_{w_{\max}} - x_{w_{\min}}}$$

$$\frac{y_v - y_{v_{\min}}}{y_{v_{\max}} - y_{v_{\min}}} = \frac{y_w - y_{w_{\min}}}{y_{w_{\max}} - y_{w_{\min}}}$$

$$S_x = \frac{x_{v_{\max}} - x_{v_{\min}}}{x_{w_{\max}} - x_{w_{\min}}}$$

$$S_y = \frac{y_{v_{\max}} - y_{v_{\min}}}{y_{w_{\max}} - y_{w_{\min}}}$$



Where  $S_x, S_y$  are scaling factors

# Clipping



- Any procedure that identifies those portions of a picture that are either inside or outside of a specified region of space is called clipping.

## Point Clipping

Clip window is a rectangle in standard position, we save a point

$P = (x, y)$  for display if the following inequalities are satisfied:

- The edges of the clip window ( $xW_{min}$ ,  $xW_{max}$ ,  $yW_{min}$ ,  $yW_{max}$ ) can be either the world-coordinate window boundaries or viewport boundaries.
- If any one of these four inequalities is not satisfied, the point is clipped .

$$xW_{min} \leq x \leq xW_{max}$$

$$yW_{min} \leq y \leq yW_{max}$$

## Line Clipping

- First, test a given line segment to determine whether it lies completely inside or completely outside the clipping window.
- If line is not completely inside or completely outside, perform intersection calculations with clipping boundaries.
- Here use inside-outside test .

# Line Clipping

## Cohen-Sutherland Line Clipping

- To clip a line, we need to consider only its endpoints.
- If both endpoints of a line lie inside the window, the entire line lies inside the window. No clipping is required.

## Inside-Outside Window Codes

- Each of the nine regions associated with the window is assigned a 4-bit code to identify the region
- 1.If both endpoints of line have a region code **0000** then accept this line.
  - 2.Else, perform the logical **AND** operation for both region codes. If the result is not **0000**, then reject the line.

|      |                       |      |
|------|-----------------------|------|
| 1001 | 0001                  | 0101 |
| 1000 | 0000<br><b>Window</b> | 0100 |
| 1010 | 0010                  | 0110 |

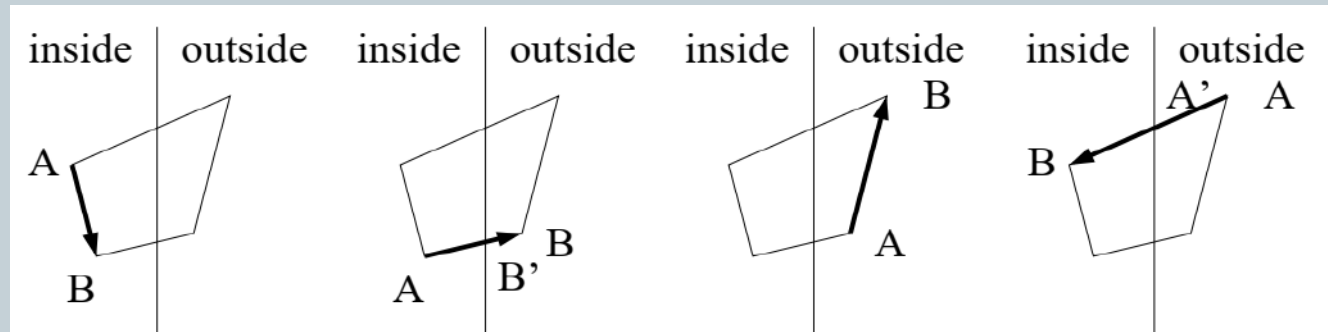
Else you need clipping.

- ✓ Choose an endpoint of the line that is outside the window.
- ✓ Find the intersection point at the window boundary based on region code .
- ✓ Replace endpoint with the intersection point and update the region code.
- ✓ Repeat step 1 until we find a clipped line either trivially accepted or trivially

# Sutherland - Hodgeman Polygon Clipping



- The Sutherland - Hodgeman algorithm performs a clipping of a polygon against each window edge in turn.
- There are four possible cases when processing vertices sequence around the perimeter of a polygon
- Assuming vertex A has already been processed,
  - Case 1 — vertex B is added to the output list
  - Case 2 — vertex B' is added to the output (edge AB is clipped to AB')
  - Case 3 — no vertex added (segment AB clipped out)
  - Case 4 — vertices A' and B are added to the output (edge AB is clipped to A'B)





# 3D Object Representation



- A two dimensional(2D) object is an object that has two dimensions such as length and width only and no thickness or height.
- A three dimensional object is an object with three dimensions :a length, width and height or depth.
- Representation schemes for solid objects are:
  - ✓ Boundary Representation (B-reps)
  - ✓ Space Partitioning representation:

**Boundary Representation ( B-reps):**  
It describes a three dimensional object as a set of surfaces that separate the object interior from the environment.  
Eg: polygon facets and spline patches.

**Space Partitioning representation:**  
It describes the interior properties, by partitioning the spatial region containing an object into a set of small, non overlapping, contiguous solids(usually cubes). Eg: Octree Representation.

# 3D Transformations

## Translation

- Translate a 3D point by adding translation distances,  $t_x$ ,  $t_y$  and  $t_z$ , to the original coordinate position  $(x,y,z)$ :

$$x' = x + t_x \quad y' = y + t_y$$

$$z' = z + t_z$$

Transformation matrix is,

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

## Scaling (w.r.t the Origin)

- Here scaling factors  $S_x$ ,  $S_y$  and  $S_z$ , which are multiplied to the original vertex coordinate positions  $(x,y,z)$ :

$$x' = x * S_x \quad y' = y * S_y$$

$$z' = z * S_z$$

Transformation matrix is,

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

# 3D Transformations

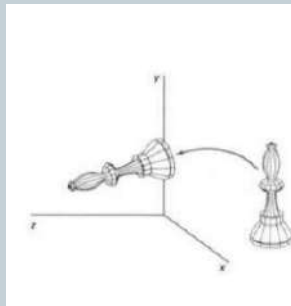
## Rotation

- A 3D rotation can be specified around any line in space.

### X axis Rotation

The equation for X-axis rotation

$$\begin{aligned} x' &= x \\ y' &= y \cos\theta - z \sin\theta \\ z' &= y \sin\theta + z \cos\theta \end{aligned}$$



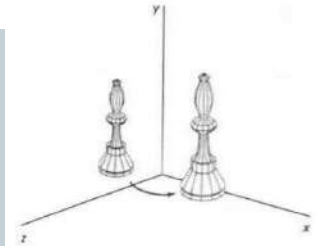
$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta & 0 \\ 0 & \sin\theta & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

### Y axis rotation

The equation for Y-axis rotation

$$\begin{aligned} x' &= x \cos\theta + z \sin\theta \\ y' &= y \\ z' &= z \cos\theta - x \sin\theta \end{aligned}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & 0 & \sin\theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin\theta & 0 & \cos\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

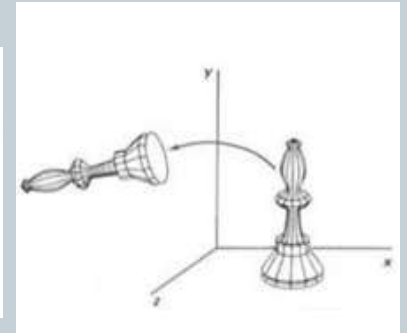


### Z axis Rotation

The equation for z-axis rotation

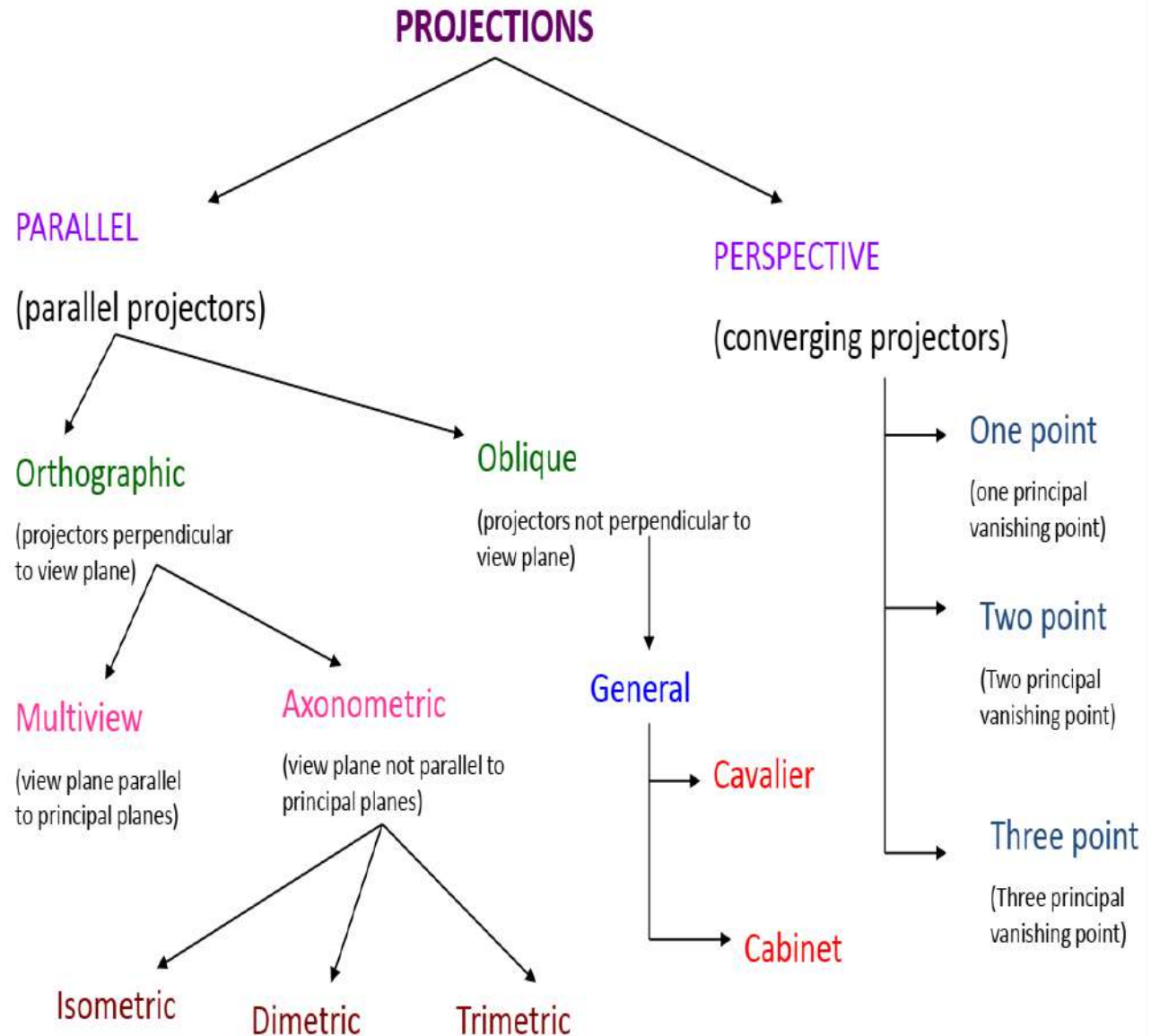
$$\begin{aligned} x' &= x \cos\theta - y \sin\theta \\ y' &= x \sin\theta + y \cos\theta \\ z' &= z \end{aligned}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta & -\sin\theta & 0 & 0 \\ \sin\theta & \cos\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$



# Projections

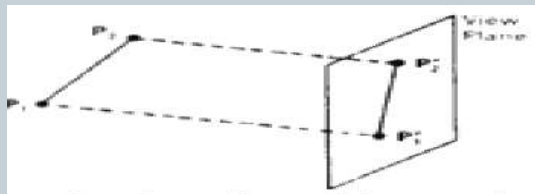
Projection means transformation of a three dimensional area into two dimensional area.



# Projections

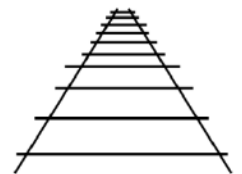
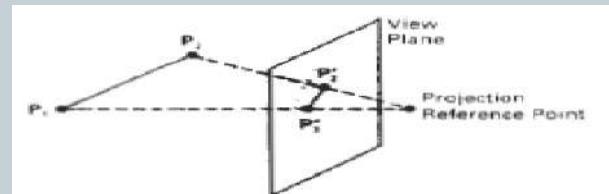
## Parallel Projection

- In parallel projection, co-ordinates positions are transformed to the view plane along parallel lines.
- Not give us a realistic representation of the appearances of 3D objects ,but Preserves relative proportions of objects.



## Perspective Projection

- In perspective projection, objects positions are transformed to the view plane along lines that converge to a point called projection reference point (centre of projection).
- Produces realistic views but does not preserve relative proportions.
- Under perspective projections, any set of parallel lines that are not parallel to the Projection plane will converge to a point called **vanishing point**.



# Parallel Projections

- In parallel projection, When the projection is perpendicular to view plane it is called orthographic projection.
- In orthographic projection when projection lines making an angle  $90^{\circ}$  with any principal axis ,it is called multi view orthographic projection.
- Otherwise, It is called is called axonometric orthographic projection.
- In axonometric projection, if the projection lines makes equal angles with the three principal axes it is isometric .
- With any two principal axes it is diametric
- Not make any equal angles with principal axes it is trimetric projection.
- When the projection lines are not perpendicular to the view plane, it is oblique projection.
- If the projection lines make an angle of  $45^{\circ}$  view plane,  $\tan \alpha = 1$  ,the views obtained are called cavalier
- When the projection angle chosen so that it is approximately  $63.4^{\circ}$ ,  $\tan \alpha = 2$ ,the resulting view is a cabinet projection.



# Hidden Surface Removal Methods



- Also called Visible Surface Detection Method
- Its major concern for identifying those parts of a scene that are visible from a chosen viewing position.

These two approaches are:

- ✓ **In object-space method:** compares objects and parts of objects to each other within the scene definition determine which surfaces, should label as visible.
- ✓ **In Image-Space methods:** Visibility is decided, point by point at each pixel position on the projection plane.  
Eg.: Z buffer Method, Scan line Method

# Hidden Surface Removal Methods



## Z Buffer Method

- It compares surface depths at each pixel position on the projection plane.
- It is called z-buffer method since object depth is usually measured from the view plane along the z-axis of a viewing system.
- The method is usually applied to scenes containing only polygon surfaces.
- In Z-buffer method, two buffers are required.
- **Depth buffer (z-buffer)**: stores the depth value for each (x, y) position as surfaces are processed.
- **Refresh buffer (Image buffer)**: stores the intensity value for each position.

## Scan line Method

- As each scan line is processed, all polygon surfaces intersecting that line are examined to determine which are visible.
- Across each scan line, depth calculations are made for each overlapping surface to determine which is nearest to the view plane.
- When the visible surface has been determined, the intensity value for that position is entered into the image buffer.
- A set of tables are set up for the various surfaces- Edge table and a Polygon table.

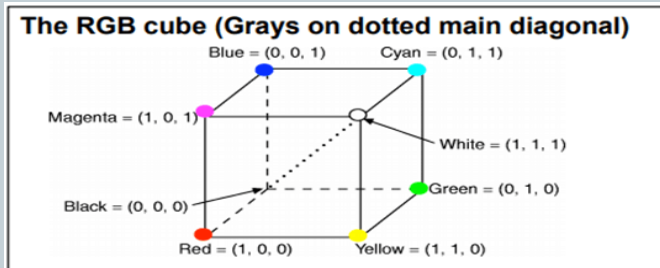
# Color Spaces



- Color spaces are the mathematical representation of a set of colors.

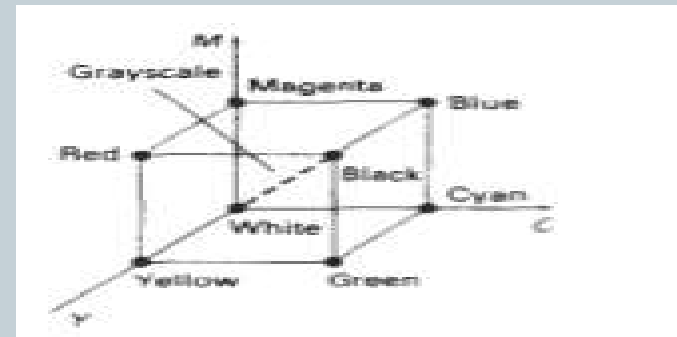
## RGB Color Space

- This theory of vision is the basis for displaying color output on a video monitor using three primary colors red, green and blue referred to as RGB model.
- Represented by the unit cube defined on R,G,B axes.



## CMY Color Model

- Defined by the primary colors Cyan, Magenta and Yellow(CMY).
- This is useful for produce a color pattern for hardcopy devices.
- A unit cube representation of the CMY model is shown as,

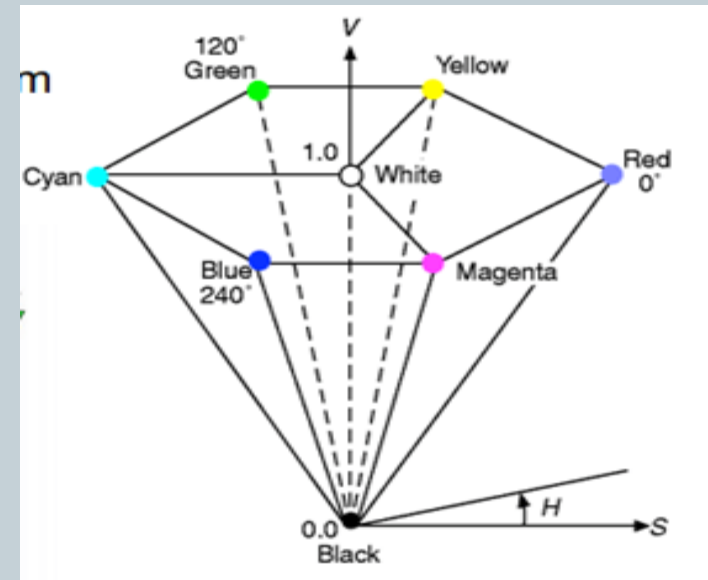


# Color Spaces

## HSV Color Model

- HSV stands for Hue, Saturation, and Value (brightness).
- To give color specifications, a user selects a color and the amount of white and black that is to be added to obtain different shades, tints, and tones.
- It is a hexcone subset of the cylindrical coordinate system.

- The vertical axis in this model is called Lightness (L).
- Saturation parameter S specifies the relative purity of a color.



# Illumination Model



- The intensity of light seen on each surface depends up on the type of light sources and the surface characteristics of the object.
- If incident light energy is reflected or transmitted, then the object is visible.

## Light Sources

- ✓ **Light Reflecting Sources:** These are the sources which reflected the illumination .
- ✓ **Light Emitting Sources**  
Eg:Sun,Bulb etc
- **Point Source :**The simplest model for light emitting is Point source. Sources that are sufficiently far from the scene can be accurately modeled as point source. For example Sun.
- **Distributed Light Source:** This occurs when we have a large nearby source. In this case, the illumination effects cannot be approximated realistically with a point source. For example –tube light.

# Basic Illumination Models & Rendering

- An **illumination model** is used to calculate the intensity of the light that is reflected at a given point on a surface.
- A **rendering method** uses intensity calculations from the illumination model to determine the light intensity at all pixels in the image.
- Rendering is the process a computer uses to create an image from a data file.

## Ambient Light

- The amount of ambient light incident on each object is a constant for all surfaces and over all directions.
- We can set the level for the ambient light in a scene with parameter  $I_a$  and each surface is then illuminated with this constant value.
- The resulting reflected light is a constant for each surface independent of the viewing direction and the spatial orientation of the surface.
- The intensity of reflected light for each surface depends on the optical properties of the surface

# Basic Illumination Models & Rendering



## Diffuse Reflection

- It is constant over each surface in a scene, independent of the viewing direction.

## Specular Reflection

- If we look at an illuminated shiny surface, we see a highlight or bright spot at certain viewing directions. This is called specular reflection.
- It is the result of total reflection of the incident light in a concentrated region around the specular reflection angle.

## Intensity Attenuation

- If two parallel surfaces with same optical parameters overlap they would be indistinguishable from each other. The two surfaces would be displayed as one surface.
- Problems by using inverse linear or quadratic functions to attenuate intensities.

# Polygon Rendering Methods



## Phong Shading

- A more accurate method for rendering a polygon surface is to interpolate normal vectors, and then apply the illumination model to each surface point.
- Also called normal vector interpolation shading.
- It greatly reduces the Mach-band effect.

### Steps:

- ✓ Determine the average unit normal vector at each polygon vertex.
- ✓ Linearly interpolate the vertex normals over the surface of the polygon.
- ✓ Apply an illumination model along each scan line to calculate projected pixel intensities for the surface points.



# Polygon Rendering Methods

## Constant-Intensity Shading (Flat Shading)

- In this single intensity is calculated for each polygon.
- All points over the surface of the polygon are then displayed with the same intensity value.
- Useful for quickly displaying the general appearance of a curved surface.

## Gouraud Shading

- Renders a polygon surface by linearly interpolating intensity values across the surface.
- Intensity values for each polygon are matched with the values of adjacent polygons along the common edges.

- Thus eliminating the intensity discontinuities that can occur in flat shading.

## Steps

- ✓ Determine the average unit normal vector at each polygon vertex.
- ✓ Apply an illumination model to each vertex to calculate the vertex intensity.
- ✓ Linearly interpolate the vertex intensities over the surface of the polygon

# Design of Animation Sequences



- **Storyboard layout :**
  - ✓ The storyboard is an outline of the action.
- **Object definitions:**
  - ✓ Given for each participant in the action.
  - ✓ Objects can be defined in terms of basic shapes
- **Key-frame specifications:**
  - ✓ A detailed drawing of the scene at a certain time in the animation sequence.
- **Generation of in-between frames:**
  - ✓ The intermediate frames between the key frames.
  - ✓ The number of in-betweens needed is determined by the media to be used to display the animation.



## **Morphing**

Transformation of object shapes from one form to another is called morphing.

## **Tweening**

The process of generating intermediate frames between two images to give the appearance that the first image evolves smoothly into the second image.

## **Image warping**

Image warping is the process of digitally manipulating an image such that any shapes portrayed in the image have been significantly distorted.

## **Zooming**

The transformation effectively scales down or blows up a pixel map or a portion of it with the instructions from the user.

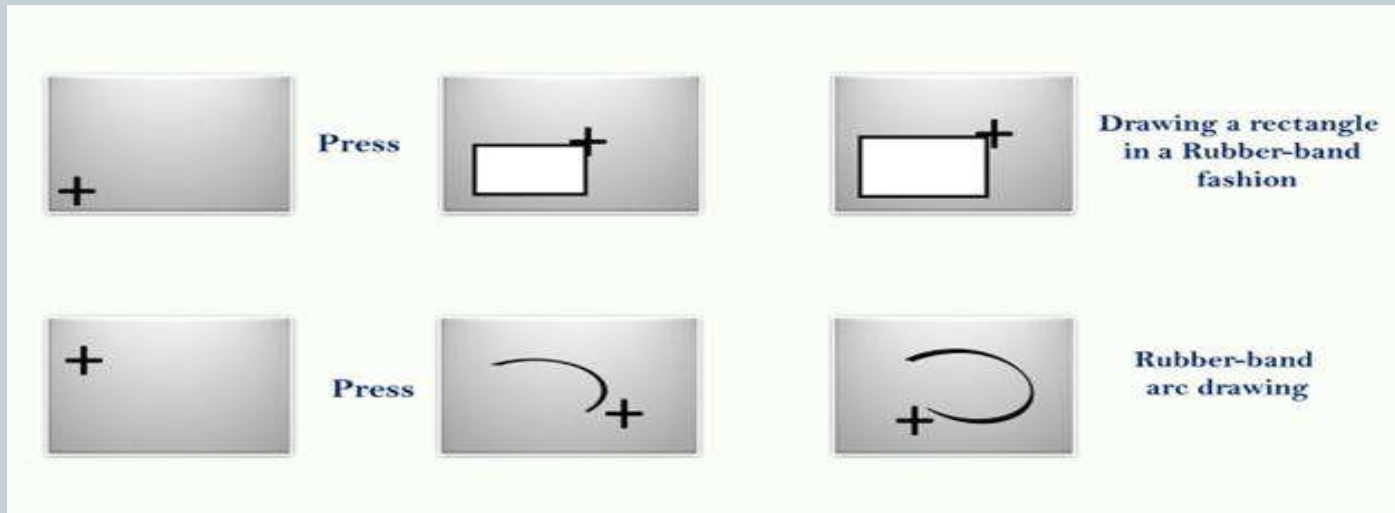
## **Panning**

- ✓ Acts as a qualifier to the zooming transformation.
- ✓ Moves the scaled up portion of the image to the center of the screen and depending on the scale factor, fill up the entire screen.



## Rubber Band Techniques

Popular technique of drawing geometric primitives such as line, polylines, rectangle, circle and ellipse on the computer screen.





*Thank You.....*